# The Transmission of Monetary Policy through Redistributions and Durable Purchases

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Workhorse models of monetary policy:

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Workhorse models of monetary policy:

- are centred on nominal rigidities (New Keynesian model)
- abstract from redistributional effects (representative agent)

Study different channel of monetary transmission. Simple DSGE model

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- monetary policy implemented through open market operations
  - contrast to "helicopter drops"

**Open Market Operation (OMO)**: central bank sells/buys short-term bonds

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  - when researchers estimate the transmission mechanisms, these effects are present...

#### Expansionary OMO triggers:

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  - breakdown Ricardian Equivalence

#### Empirical evidence

#### VectorAutoRegresson

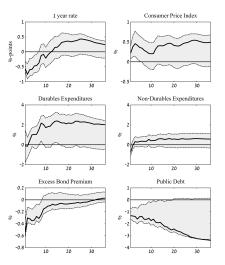


Figure: Responses to an expansionary monetary policy shock, identified following Gertler and Karadi (2015).

## Model

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- Following retirement, immediate death shock may occur.
- Population size normalized to one. Stationary population:

$$\rho_o \nu = \rho_x \left( 1 - \nu + \rho_o \nu \right)$$

where  $\nu$  is the fraction of young agents in the population (#newborn=#aging=#dying).

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- Agents can also save in bonds  $(b_t)$

• Firms are perfectly competitive, producing durables and non-durables with the same technology  $y_t = h_t$ . They rent labor on an competitive labor market. Profit maximization implies  $w_t = 1$ .

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- The treasury makes a transfer  $\tau_t^s$  to each household of type s. We denote an agent's life-cycle status by superscript  $s \in \{n, y, o\}$ , with n denoting a newborn young agent, y a pre-existing young agent, and o an old agent.

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- Wealth of deceased agents equally distributed among the young.

# Old agents

Optimization problem old agent  $(\mathbf{s} = \mathbf{o})$  in real terms:

$$\begin{split} &V^{\mathbf{o}}(\mathbf{a},\Gamma) = \max_{c,d,m,b} U(c,d,m) + \beta \left(1-\rho_{\mathbf{x}}\right) \mathbb{E} V^{\mathbf{o}}(\mathbf{a}',\Gamma') \\ &s.t. \\ &c+d+m+b = \mathbf{a}+\tau^{\mathbf{o}} \\ &\mathbf{a}' \equiv \left(1-\delta\right)d + \frac{m}{1+\pi'} + \frac{(1+r)\,b}{1+\pi'}, \\ &c.\,d.\,m > 0. \end{split}$$

where  $V^{\mathbf{o}}(a,\Gamma)$  is the value function, a denotes individual wealth,  $\Gamma$  is the aggregate state and  $\pi$  is the net rate of inflation. Also,  $\beta$  is the agents' subjective discount factor,  $\delta$  is the depreciation rate of durables and  $\mathbb E$  is the conditional expectations operator.

# Young agents

Optimization problem young agents  $(\mathbf{s} = \mathbf{n}, \mathbf{y})$ 

$$\begin{split} V^{\mathbf{s}}(\mathbf{a},\Gamma) &= \max_{c,d,m,b,h} U(c,d,m) - \zeta \frac{h^{1+\kappa}}{1+\kappa} + \beta \left(1-\rho_o\right) \mathbb{E} V^{\mathbf{y}}(\mathbf{a}',\Gamma') \\ &+ \beta \rho_o \left(1-\rho_x\right) \mathbb{E} V^{\mathbf{o}}(\mathbf{a}',\Gamma') \end{split}$$
 s.t. 
$$c+d+m+b = \mathbf{a} + \mathbf{w}h + \tau^{\mathbf{b}\mathbf{q}} + \tau^{\mathbf{s}}, \\ \mathbf{a}' &\equiv \left(1-\delta\right)d + \frac{m}{1+\pi'} + \frac{\left(1+r\right)b}{1+\pi'}, \\ c,d,m &\geq 0, \end{split}$$

where w is the wage rate and  $\tau^{\mathbf{bq}}$  is a bequest transfer. In the utility function  $\zeta>0$  is a scaling's parameter and  $\kappa>0$  determines the Frisch elasticity of labor supply.

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• To analyze monetary policy shocks, we assume that  $M_t$  is driven by an exogenous process subject to stochastic shocks.

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where the total amount of transfers is adjusted to balance the government's budget

• Net beneficiary is the government. Key how it redistributes gain.

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What arises is a representative young agent. We preserve
heterogeneity between old and young agents, as well as heterogeneity
among old agents.

# Market clearing

Market clearing constraints durables and non-durables:

$$c_t = \nu c_t^{\mathbf{y}} + (1 - \nu) c_t^{\mathbf{o}}$$
  
$$d_t = \nu d_t^{\mathbf{y}} + (1 - \nu) d_t^{\mathbf{o}},$$

Resource constraint, clearing conditions for money and bond market:

$$\begin{array}{rcl} c_t + d_t & = & \nu \, h_t^{\mathbf{y}} + (1 - \delta) \, d_{t-1}, \\ m_t & = & \nu \, m_t^{\mathbf{y}} + (1 - \nu) \, m_t^{\mathbf{o}}, \\ 0 & = & b_t^{\mathbf{g}} + b_t^{\mathbf{c}\mathbf{b}} + \nu \, b_t^{\mathbf{y}} + (1 - \nu) \, b_t^{\mathbf{o}} \\ \end{array}$$

Magnitude bequest transfer:

$$\boldsymbol{\tau}_t^{\mathbf{bq}} = \frac{\rho_{\mathbf{x}} \int\limits_{i:\mathbf{s} = \mathbf{o}} \mathbf{a}_{i,t} di + \rho_{o} \rho_{\mathbf{x}} \boldsymbol{\nu} \mathbf{a}_t^{\mathbf{y}}}{\boldsymbol{\nu}}$$

## Equilibrium

**Definition.** A recursive competitive equilibrium is defined by policy rules for non-durable consumption,  $c^{\mathbf{s}}(\mathsf{a},\Gamma)$ , durable consumption,  $d^{\mathbf{s}}(\mathsf{a},\Gamma)$ , money holdings,  $m^{\mathbf{s}}(\mathsf{a},\Gamma)$ , bond holdings,  $b^{\mathbf{s}}(\mathsf{a},\Gamma)$ , labor supply,  $h^{\mathbf{s}}(\mathsf{a},\Gamma)$ , with  $\mathbf{s}=\mathbf{n},\mathbf{y},\mathbf{o},\mathbf{cb},\mathbf{g}$ , as well as laws of motion for inflation, the nominal interest rate and the real wage, such that

- households optimize their expected life-time utility subject to their constraints and the law of motion for the aggregate state,
- the treasury and central banks follow their specified policies,
- the markets for bonds, money, goods and labor clear in every period.

The aggregate state  $\Gamma$  includes the value of the monetary policy shock, the distribution of wealth among agents, as well as the initial holdings of assets by households, the treasury and the central bank.

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- Given the transfers to newborns, the model becomes observationally equivalent to one with an infinitely-lived representative agent with subjective discount factor  $\widetilde{\beta}=\beta\,(1-\rho_o)$ .
- Easy to show that monetary policy becomes neutral with respect to real activity when utility is separable in money and consumption. No wealth effects (Weil (1991)).

# Monetary neutrality

- Following arguments similar to Sidrauski (1967) one can show that, provided that money and goods enter the utility function separably, monetary policy does not affect real outcomes.
- To show this, consider the representative agent's first-order conditions for durables, labor supply, and the aggregate resource constraint:

$$\begin{array}{rcl} U_{c,t} & = & U_{d,t} + \widetilde{\beta} \left(1 - \delta\right) \mathbb{E}_t U_{c,t+1} \\ U_{c,t} & = & \zeta h_t^{\kappa} \\ c_t + d_t & = & h_t + \left(1 - \delta\right) d_{t-1} \end{array}$$

where  $U_{c,t}$  and  $U_{d,t}$  are, respectively, the agents' marginal utilities with respect to non-durables and durables.

 Under preference separability, this is a closed dynamic system of 3 equations and 3 endogenous variables. No nominal variables enter this system.

# Adding search and matching frictions

- Diamond-Mortensen-Pissarides style matching friction.
- Young workers live in representative family, as in Merz (1995) and Andolfatto (1996).
- Workers are born without a job, lose job with fixed probability. Search for jobs when unemployed, accept any job offer in equilibrium.
- ⇒ shut off labour supply chanel. Employment determined by firms' endogenous vacancy posting decision. ⇒ worker-firm relationships are durables.

# Quantitative implementation

#### Computation

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- Models with wealth heterogeneity and aggregate fluctuations typically difficult to solve, because wealth distribution is part of the economic state (Krusell and Smith (1998)).
- Despite the presence of heterogeneity, our model can be solved using standard methods (first-order perturbation), under the following preferences:

$$U(c_{i,t}, d_{i,t}, m_{i,t}) = \frac{u_{i,t}^{1-\sigma} - 1}{1-\sigma},$$

$$u_{i,t} \equiv \left[c_{i,t}^{\frac{\epsilon-1}{\epsilon}} + \eta d_{i,t}^{\frac{\epsilon-1}{\epsilon}} + \mu m_{i,t}^{\frac{\epsilon-1}{\epsilon}}\right]^{\frac{\epsilon}{\epsilon-1}},$$

 $\sigma$ ,  $\epsilon$ ,  $\eta$ ,  $\mu > 0$ . Baseline:  $\sigma = \epsilon = 1$  (separability).

# Shock process

Money growth rule:

$$\frac{M_t}{M_{t-1}} = 1 + z_t$$

where  $z_t$  is a mean reverting process following:

$$z_t = \xi(\overline{m} - m_{t-1}) + \varepsilon_t, \ \xi \in [0, 1),$$

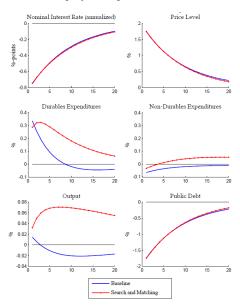
where  $\varepsilon_t$  is an i.i.d. shock innovation. (Implicit inflation target is zero.)

# Parameter values (quarterly model)

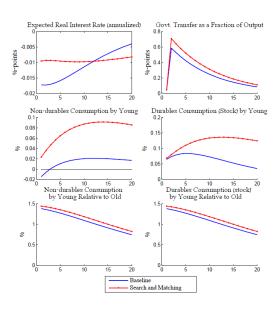
Table 1. Parameter values for the baseline model and the Search and Matching (SaM) model.

	baseline	SaM	description	motivation
β	0.9732	0.9755	subjective discount factor	4% s.s. annual interest rate
$\eta$	0.31	0.31	durables preference param.	20% s.s. spending on durables (NIPA)
$\mu$	0.0068	0.0049	money preference param.	1.8 s.s. M2 velocity $(\frac{y}{m})$ (FRB/NIPA)
$\sigma$	1	1	coef. rel. risk aversion	convention literature
$\epsilon$	1	1	intratemp. elast. of subst.	convention literature
$\kappa$	1	_	inv. elasticity labour supply	convention literature
ζ	0.5795	_	disutility of labor	normalize agg. output to one
$\rho_o$	0.0063	0.0063	ageing probability	avg duration working life 40 years
$\rho_x$	0.0125	0.0125	death probability	avg duration retirement 20 years
$\delta$	0.04	0.04	depreciation rate durables	Baxter (1996)
$b_0^g$	-2.4	-2.4	initial bonds Treasury	government debt $60\%$ of annual output
$b_0^{cb}$	0	0	initial bondsCentral Bank	no initial central bank debt/bonds
ξ	0.2	0.4	coefficient monetary rule	half life nominal interest rate $2.5~{\rm years}$
$\chi_0$	_	0.0044	variable hiring cost	$\chi_1/\chi_0=10$ (Pissarides (2009))
$\chi_1$	_	0.0004	fixed hiring	$\chi_1/\chi_0=10$ (Pissarides (2009))
$\alpha$	_	0.5	matching function elasticity	convention search literature
$\nu$	_	0.7	scaling matching function	vacancy filling probability 0.74

# Expansionary monetary policy shock

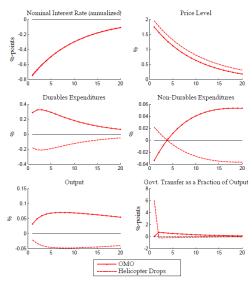


#### Young versus old



## Monetary expansion

#### OMO vs helicopter drop



#### Conclusions

- Simple life-cycle DSGE model without nominal rigidities
- Responses to monetary policy shocks in line with VAR evidence: key role for durables
  - can help the NK model in fitting the data
- Transmission mechanism: two redistributional channels:
  - Among households
  - Between households and government
- Implementation of monetary policy matters (OMO vs helicopter drop)