

**discussion of "Complex Methods in Economics: An Example of Behavioral Heterogeneity in House Prices"**  
**by Bolt, Demertzis, Diks and Van der Leij**

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# The paper

## Goal:

- Theory of (nonlinear) booms and crashes in housing markets
- Early warning indicators

## Tool:

- Estimated asset-pricing model with heterogeneous beliefs

## Results:

- Empirical support for belief heterogeneity
- Possibility of multiple equilibria

# My discussion

- Alternative motivation
- Model
- Implications
- Suggestions

# What's wrong with standard models?

## Off-the-shelf equilibrium model with rational expectations

- Households:

$$\max_{(c_t, h_t)_{t=0}^{\infty}} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \{ \ln c_t + \gamma \ln h_t \}$$

s.t.

$$c_t + p_{h,t} (h_t - h_{t-1}) = y_t$$

where  $c_t$  is consumption,  $p_{h,t}$  is the house price,  $h_t$  is housing,  $y_t$  is income and  $\gamma, \beta \in (0, 1)$  are preference parameters.

- Housing supply:

$$h_t = h$$

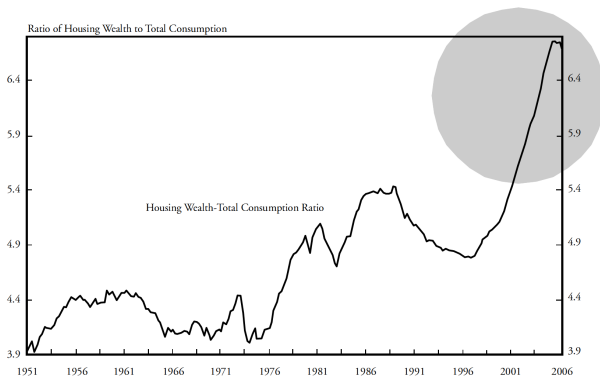
# What's wrong with standard models?

House-price equation:

$$\begin{aligned}\frac{p_{h,t}}{c_t} &= \frac{\gamma}{h} + \beta \mathbb{E}_t \frac{p_{h,t+1}}{c_{t+1}} \\ &= \frac{\gamma}{h(1-\beta)}\end{aligned}$$

$\Rightarrow$  **constant** ratio of housing wealth to consumption  $\frac{p_{h,t}h}{c_t}$ .

# What's wrong with standard models?



Source: Ludvigson (2007)

# What's wrong with standard models?

$$\frac{p_{h,t}}{c_t} = \frac{\gamma}{h} + \beta \mathbb{E}_t \frac{p_{h,t+1}}{c_{t+1}}$$

- DSGE literature: introduce collateral constraints + shocks to preference parameter  $\gamma$
- This paper: free up expectation  $\mathbb{E}_t$

# Beliefs and house prices

## Exciting new literature

- Burnside, Eichenbaum and Rebelo (2011): "infectious" beliefs about house price fundamentals
- Adam, Kuang and Marcet (2011): learning about expectations
- Bolt, Demertzis, Diks and Van der Leij (2011): estimated model with belief heterogeneity and endogenous switching



# The model

- equilibrium asset pricing model of the housing market
- all agents know the *fundamental* house price
- 2 types of agents with different expectations about *actual* house price developments
- exogenous process for rents, constant interest rate

## Excess return on housing

$$\underbrace{R_{t+1}}_{\text{excess return}} = \underbrace{Q_t}_{\text{rent}} + \underbrace{(P_{t+1} - P_t)}_{\text{capital gain}} - \underbrace{P_t r}_{\text{foregone interest}}$$

- Excess return compensates homeowners for taking risk
- Alternative interpretation: return that is needed to make agents indifferent between owning and renting

# Housing demand

- Being a mean-variance investor, the demand for housing of a type- $h$  agent is given by:

$$z_{h,t} = \frac{\mathbb{E}_{h,t}R_{t+1}}{\alpha V}$$

- ⇒ housing demand proportional to expected excess return, according to subjective beliefs
- ⇒ pessimistic agents may go short in housing

# Behavioral assumptions

- 1 Expectations formation of type- $h$  agent:

$$\mathbb{E}_{h,t} X_{t+1} = \theta + \phi_h X_{t-1} \quad h = 1, 2$$

where  $X_t = P_t/P_t^f - 1$ , with  $P_t^f$  being the fundamental house price.

- 2 Fraction of agents switching between the two types is an exogenous function of past forecasting performance.

# Estimation

	United States	Netherlands
$\phi_1$	0.89	0.99
$\phi_2$	1.13	1.04

# Interpretation of the coefficients

Q How do type-1 and type-2 agents expect house prices to develop over the next two years?

# How much belief heterogeneity?

Expected change in house prices over the next two years

Expectation of house price growth after  $k$  quarters:

$$\mathbb{E}_{1,t} \frac{P_{t+k}}{P_t} = \left( 1 + \phi_1^{k/2} \cdot \frac{P_t - P_t^f}{P_t^f} \right) (1 + g)^k \frac{P_t^f}{P_t}$$

where  $g$  is the quarterly growth rate of the fundamental house price which I set equal to 0.5%.

# How much belief heterogeneity?

## Expected change in house prices over the next two years

- currently 5% overvaluation:

	United States	Netherlands
type-1 agent	+2%	+4%
type-2 agent	+7%	+5%

- currently 25% overvaluation:

	United States	Netherlands
type-1 agent	-4%	+3%
type-2 agent	+17%	+8%

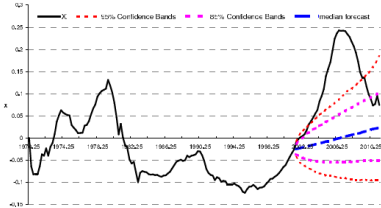


# What about trade volumes?

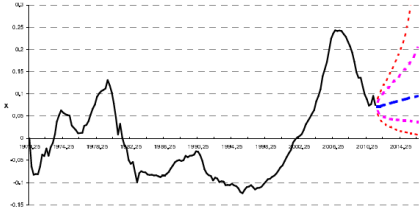
- strong belief heterogeneity  $\Rightarrow$  many housing trades?
- how does the volume of housing trades fluctuate over the housing cycle?
- Idea: simulate individual agent

# Forecasting power?

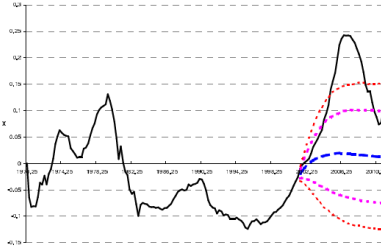
USA - BHM insample forecasts



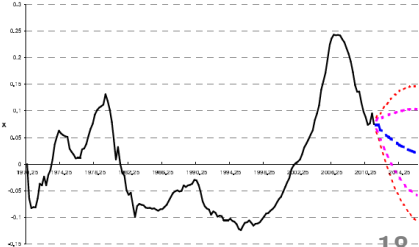
USA - BHM out of sample forecasts



USA - AR in sample forecasts



USA - AR out of sample



## More modest objective

- Does the introduction of the belief heterogeneity improve the model's ability to explain observed cyclical patterns in house price data?

# Conclusion

- Exciting new work on housing!
  - What do we learn about house prices from the model? When to declare empirical success?
  - Relax assumption of housing as pure asset? Short-selling restrictions?
  - Implications for housing trades?
  - Robustness over different forecasting and switching rules? Include rational agent in the model?